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# Determination of Refractive Index Gradient and Diffusion Coefficient of Salt Solution from Laser Deflection Measurement

#### I. Introduction

Diffusion is a process involving random walk of atoms or molecules leading a system towards its thermodynamic equilibrium. For instance, if a vessel contains a mixture of water and a salt solution, there will be a diffusive flux of salt molecules from regions of high salt concentration towards regions of lower salt concentration. The diffusion rate is characterized by the diffusion coefficient D. Diffusion plays a major role in a wide range of processes, from biochemistry to astrophysics. In the following experimental problem, diffusion of salt molecules is studied. Salt molecules will move diffusively from a salt solution towards the region with distilled water, creating a transition layer of variable salt concentration. The refraction index of this solution depends on the salt concentration. Therefore, we can study diffusion process through optical experiments using laser beam deflection method.

## II. Objectives

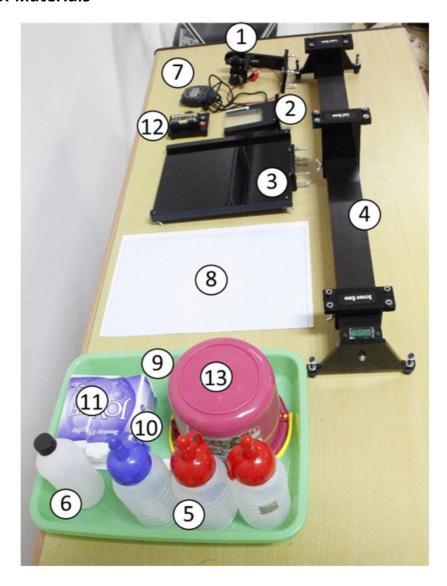
1. To determine the diffusion coefficient of salt-water solution in water by measuring the gradient of refractive index.

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2. To determine the rate of change of the diffusion coefficient to the change of salt solution concentrations.

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#### III. List of Materials



**Figure 1.** Materials for this experiment.

- 1. Line Laser Module (Diode laser with  $\lambda$  = 632 nm and cylindrical lens)
- 2. Diffusion cell (6.5 cm x 0.8 cm x 9.5 cm) with holder)
- 3. Screen with holder
- 4. Optical rail with length scale
- 5. Salt-water Solutions
- 6. Distilled Water (Aquadest)
- 7. Stopwatch
- 8. Paper with scale (block millimeter paper)

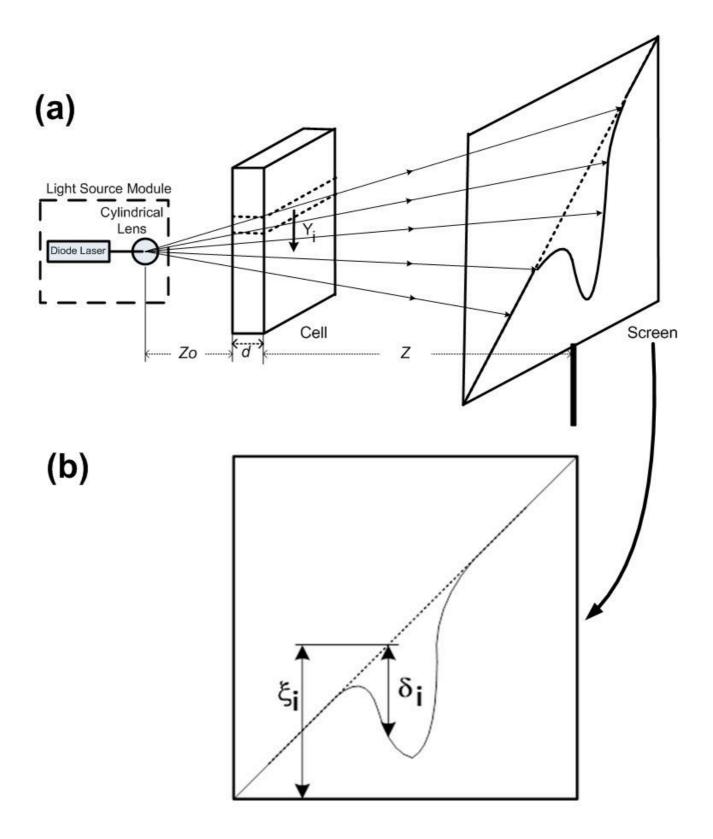
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- 9. Pipette (dropper)
- 10. Knife + Tissue for cleaner
- 11. Tissue
- 12. Battery
- 13. Buckets as waste container of salt and water solution

The schematic diagram of the experimental set-up can be seen in Figure 2.



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**Figure 2. (a)** Schematic diagram of the experiment. **The cell contains salt water solution with distilled water (aquadest) above it. (b)** Typical deflactogram, the deflected laser beam that appears on the screen when the diffusion between the solution 1 and solution 2 occurs.

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To obtain a profile of the refractive index gradient as a function of vertical position in the fluid we must relate the vertical position on the screen  $(\xi)$  to the vertical height in the cell (Y), and relate the vertical deflection  $(\delta)$  to the gradient of refractive index (dn/dY). From the geometry of the experimental setup (see Figure 2) we have:

$$Y_i = \frac{\xi_i Z_0}{Z_0 + d + Z} \tag{1}$$

where  $Z_0$ , Z and d that are shown in Figure 2(a) denote the distance between the light source module and the diffusion cell, the distance between the diffusion cell and the screen, and the diffusion cell's thickness, respectively. For measuring  $Z_0$ , the line marked on the laser module stand indicates the position of the cylindrical lens.

The thickness of the cell (d) and the refractive index gradient are both small enough so that the refraction produces negligible vertical displacement of the ray within the cell. In this limit each ray travels at nearly constant vertical height within the cell and is deflected by a single refractive gradient associated with this height.

It can be shown that:

$$\left(\frac{dn}{dY}\right)_i = \frac{\delta_i}{Zd} \tag{2}$$

#### **Experimental Procedures:**

• In order to obtain the deflected laser trace on the screen (as in Figure 2b) you must assemble all the components depicted in Figure 1 by following the schematic shown in Figure 2(a).

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- Ensure that the laser is on and its spot and its projection on the screen have diagonal form when it hits perpendicularly the diffusion cell. You may adjust Z,  $Z_0$ , and the focal length of the laser (by rotating the back of the laser) in order to obtain a bright and focussed line. You can also adjust the direction of the diagonal line on the screw by rotating the laser as a whole (release the laser using the screw on top). In the condition without any water or salt solutions you will see the straight diagonal laser beam.
- Deflected laser trace will appear when the two different solutions are diffusively mixed. Ensure that you pour the salt solution first into the diffusion cell container up to the limit which is marked by white line. Drop the water into the container slowly about 40 drops down the side channel using a pipette, after which you may turn on the stop watch to measure the evolution time of diffusion profile. If the set up of Z,  $Z_0$  and the height of the laser are already optimized, the deflacted laser trace on the screen will be centered, clear and the depth of the dip as large as possible. You need to find this optimum set-up in order to minimize the error of the measurement.
- After the evolution time of 30 minutes you may draw the laser trace into millimeter block paper attached to the screen using a pencil. Note that in this experiment, you will be asked to do the measurement for 3 different salt solution concentrations (i.e.  $C_0 = 23 \text{ g/150 ml}$ ,  $C_0 = 28 \text{ g/150 ml}$  and  $C_0 = 33 \text{ g/150 ml}$ ) so that you need to replace the millimeter block frequently. The millimeter block paper should be inserted to the screen and it can be loosen or tighten by rotating the screw attached in the corner of the screen.
- Please make sure that you have written your student code number and the concentration of the solution that you used on this millimeter block paper.

#### IV. Experiments and Tasks

#### A: Measurement of Refractive Index Gradient of Salt Water Solution (4.5 points)

You need to perform the steps below for all three salt concentration. Note that no error estimation is needed.

A.1	Perform the experiment to obtain the deflected laser trace on the screen. Duplicate the laser trace into the millimeter block paper attached to the screen using a pencil for evolution time of the diffusion $(t)$ of 30 minutes.	1.2 pt.
A.2	Measure $Z$ , $d$ , $Z_0$ , $\xi_i$ and $\delta_i$ (with $i$ = 1,,20, are the data points corresponding to different horizontal position) from the laser trace in the millimeter block for evolution time of the diffusion ( $t$ ) of 30 minutes. The parameters $Z$ , $d$ , $Z_0$ , $\xi_i$ and $\delta_i$ are stated in cm. Note that $Z$ , $d$ and $Z_0$ are the same for all measurement. Record the results in the Table 1.	1.5 pt.
	Calculate $Y_i$ and $\left(\frac{dn}{dY}\right)_i$ (with $i$ = 1,, 20, are the data points) for duration time of	

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A.3	diffusion $(t)$ of 30 minutes. Note that $Z$ , $d$ and $Z_0$ are the same for all measurement. Record the results in Table 2. Plot $\left(\frac{dn}{dY}\right)_i$ vs. $Y_i$ for $t$ = 30 minutes.	1.5 pt.
A.4	Determine the $Y_i$ at $\left(\frac{dn}{dY}\right)_i$ maximum obtained from question A3. Assign this $Y_i$ as $h$ .	0.3 pt.



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## **B:** Determination of Diffusion Coefficient (4.2 points)

The curves found from question A.3 can be fitted using the following equations:

$$\left(\frac{dn}{dY}\right)_i = \left(\frac{dn}{dC}\right) \left(\frac{dC}{dY}\right)_i \tag{3}$$

$$\left(\frac{dC}{dY}\right)_i \approx \frac{C_o}{2\sqrt{\pi Dt}} e^{-\frac{(h-Y_i)^2}{4Dt}}$$
 (4)

where C,  $C_0$ , D, t, h denoted as concentration, initial salt solution concentration, diffusion coefficient, duration time of diffusion, and  $Y_i$  at maximum of refractive index gradient (dn/dY), respectively. Note that (dn/dC) is constant. The diffusion coefficient can be obtained by using equations (3) and (4) to form a linear relation between  $(dn/dY)_i$  and  $Y_i$ .

B.1	Based on Eqns (3,4), find such functions $f\left(\frac{dn}{dY}\right)$ and $g\left(Y\right)$ that the dependence between $f\left(\frac{dn}{dY}\right)$ and $g\left(Y\right)$ would be linear.	0.9 pt.
B.2	Make a table (Table 3 in the answer sheet) that contains the data points, abscissa axis, ordinate axis of linear equation from B1 for dataset taken from Tasks A. Plot this table.	1.8 pt.
B.3	Determine the diffusion coefficient $D$ from linear plot obtained from B2 for data set at $t$ = 30 minutes. Note that linear dependence may hold only for a subrange of your data.	1.5 pt.

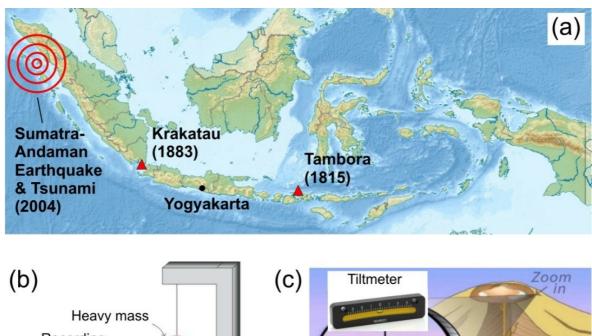
## C. Nonlinear diffusion (1.3 points)

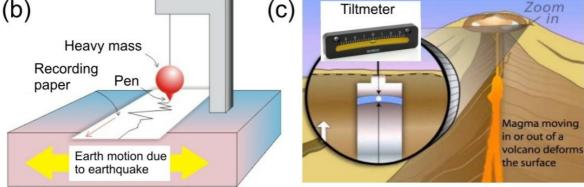
C.1	The analysis above is based on the assumption that $D$ is independent of $C$ . If this is not true, we have so-called nonlinear diffusion. However, near the maximum of $\frac{dn}{dY}$ we can consider this as an ordinary diffusion, with diffusion coefficient corresponding to the local value of concentration. Determine the rate of change of the diffusion coefficient with the change of salt solution concentration graphically using data from part B.	
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# Parallel Dipole Line Magnetic Trap for Earthquake and Volcanic Sensing

#### A. Introduction





**Figure. 1** (a) Map of Indonesia showing its well-known disasters. (b) Basic seismometer to detect earthquake. (c) Tiltmeter to monitor volcano.

Indonesia is the world's largest archipelago, with about 17,000 islands sprawling in the tropics and thus often called "the jewel of the equator". Unfortunately, it has plenty of natural threats such as earthquake and volcanic eruptions. Colossal catastrophic events (Fig. 1a) such as the Sumatra-Andaman earthquake and tsunami (2004), Krakatau (1883) and Tambora (1815) volcanic eruptions are among the deadliest disasters in the recorded history of the world. To detect earthquake, we use a *seismometer*, usually a pendulum-based system to *measure the ground displacement or acceleration* (Fig. 1b). To monitor volcano, we use *tiltmeter* to detect a change in *ground inclination* due to underground magma movement (Fig. 1c). In this problem we will explore the physics and applications of a new kind of magnetic trap and sensor-called *Parallel Dipole Line* (PDL) trap system - for sensing earthquake and to monitor volcano.

Parallel dipole line system is an arrangement of two linear distribution of magnetic dipole (also called  $\alpha$ 

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dipole line) as shown in Fig. 2. Recently two Indonesian physicists discovered a very interesting effect in this system: if the length of the dipole line is longer than certain critical length the magnetic field becomes stronger on the edges which produces a "camelback potential" as shown in Fig. 2a.\* This "camelback effect" is important as it enables this system to serve as a new type of magnetic trap called Parallel Dipole Line (PDL) trap. Experimentally we can realize this PDL trap using a pair of diametric magnets i.e. a cylinder magnets with magnetization along diameter as shown in Fig. 2c where the north and south poles are on the curved sides instead of the flat faces.

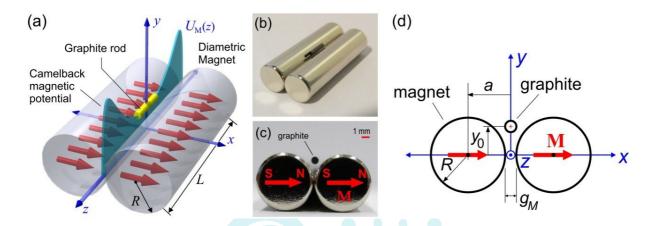


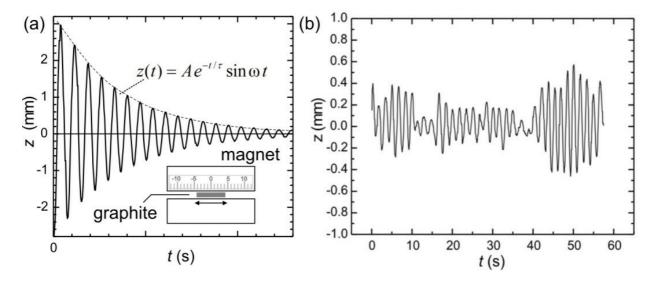
Figure 2. (a) Parallel dipole line trap model with the camelback potential along z-direction. (b) Experimental setup using "diametric" magnets. (c) Cross section view. (d) Schematics of the PDL trap. [\* Gunawan and Virgus, J. Appl. Phys. 121, 133902 (2017)].

If we drop a graphite rod (ordinary pencil lead) into the trap it will levitate or gets trapped in a stable condition. This occurs because in x-direction the graphite is repelled by the magnets from both sides and in vertical (y) direction the magnetic repulsion force balance the gravity making it levitates at height  $y_0$ (Fig. 2d). In longitudinal direction (z) the camelback potential holds the graphite stable.

The camelback potential of the magnetic trap serves as a one-dimensional oscillator. If you give a little perturbation along the z-axis to the graphite rod, it will exhibit underdamped oscillation as shown in Fig. 3a. This PDL trap can be used as a sensitive seismometer. If the ground underneath shakes, the graphite rod tends to remain stable and its relative displacement (Fig. 3b) is the "earthquake" signal. Similarly, it can also be used as sensitive tiltmeter: if you tilt the trap slightly, the graphite rod will move significantly without any friction.

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**Figure 3.** (a) Underdamped oscillation of a graphite rod along the camelback potential. (b) Seismometer application:

Ground vibration detection by PDL trap.

We will now investigate the physics and application of this PDL trap in two sections.

#### **Section A: Basic characteristics**

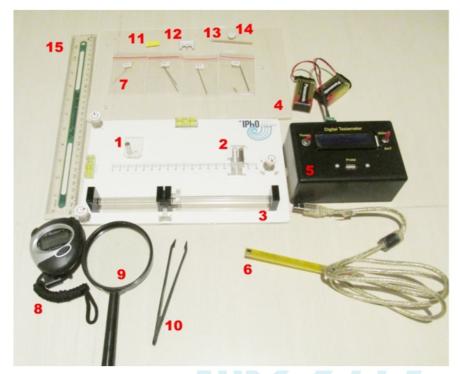
- (1) Determination of the magnet's magnetization M (2.5 pt.)
- (2) Magnetic levitation and magnetic susceptibility  $\chi$  (1.0 pt.)
- (3) The camelback potential oscillation and magnetic susceptibility  $\chi$  (1.0 pt.)
- (4) Oscillator quality factor Q and determination of air viscosity  $\mu_A$  (3.0 pt.)

#### **Section B: Applications**

- (5) PDL Trap Seismometer (0.5 pt.)
- (6) PDL Trap Tiltmeter (2.0 pt.)

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# **B.** Apparatus





Single diametric magnet



The PDL magnetic trap

Figure 4. The experimental setup.

- 1. Single diametric magnet assembly. Yellow sticker is attached to mark magnetization.
- 2. The PDL magnetic trap assembly, shown with levitating graphite. Please do not remove the magnets from the assembly.
- 3. Top platform with 3 screws
- 4. Bottom platform
- 5. Tesla meter to measure magnetic field. Batteries are provided to power up the Tesla meter and a cable to connect the Hall probe to Tesla meter.
- 6. Hall sensor probe of the Tesla meter
- 7. Graphite rods (pencil leads) with 4 diameter sizes HB/0.3, HB/0.5, HB/0.7, and HB/0.9. See the constants and data for exact diameters. You may need to break these graphite rods to specific lengths as required.
- 8. Stopwatch
- 9. Magnifying glass
- 10. Tweezer, anti-static

Experiment
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- 11. Round yellow sticker—to mark the magnetization direction (north-south pole) of single magnet
- 12. "Insert-ruler" to measure graphite levitation height
- 13. Toothpick to move around the graphite rod
- 14. Silly putty to stick magnet assemblies to platform
- 15. Ruler

#### **INSTRUCTIONS & WARNING:**

- 1. <u>Keep the single magnet and the PDL trap (double magnet) assemblies away from each other.</u>

  They can hit each other and crack!
- 2. Turn off the Tesla meter if not in use to save battery!
- 3. Please detach items 7, 11-14 carefully from bottom platform (item 4) and then place the top platform (item 3) on the bottom platform.
- 4. You can use the three screws to adjust the level of the top platform.

#### **CONSTANTS AND DATA:**

Radius of the diametric magnet : R = 3.2 mmLength of the diametric magnet : L = 25.4 mmGap of the PDL trap :  $g_M = 1.5 \text{ mm}$ 

Room temperature : T = 298 K

Magnetic permeability in vacuum :  $\mu_0 = 1.257 \times 10^{-6}$  H/m

Boltzman constant :  $k_B = 1.38064852 \times 10^{-23} \text{ m}^2 \text{ kg/s}^2 \text{ K}$ 

Acceleration of gravity :  $g = 9.8 \text{ m/s}^2$ 

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#### C. Experiment & Questions

#### SECTION A. BASIC CHARACTERISTICS OF THE PDL TRAP

## [1] Determination of the magnet's magnetization (M) (2.5 pt.)

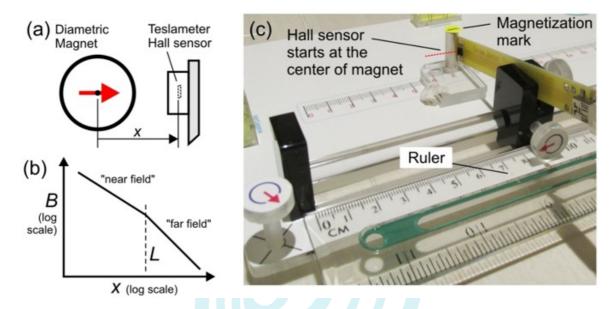


Figure 5. (a) Measuring the magnetic field. (b) Magnetic field profile (c) Setup.

The strength of the magnetic trap depends on the total magnetic dipole moment of the magnet m. It depends on the magnetization M which is magnetic dipole per unit volume and a characteristics of the magnetic material. For our cylindrical magnet:

$$M = \frac{m}{\pi R^2 L} \tag{1}$$

where R is the radius and L is the length of the magnet (see Constants and Data). The value of M is considered the same for all magnets in this experiment. We will study the magnetic field profile and the determine M of the diametric magnet used in our PDL trap.

Take <u>the single</u> diametric magnet assembly and setup the experiment as shown in Fig. 5c. Align the magnetization (as shown in Fig. 6a) pointing towards the Hall (magnetic field) sensor. Measure the strength of the magnetic field along the x-axis using Tesla meter. The magnetic field profile B in near field or "Dipole Line" limit for approximately  $x \le 16$  mm:

$$B_I(x) = \frac{\mu_0 m}{2\pi x^P I}$$
 (2)

The x-axis is along the magnetization axis of the diametric magnet as shown in Figure 6a and x refers to the distance from the center of diametric magnet to hall probe sensor inside the sensor chip. Please refer to issue of offset shown in Figure 6b.

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We will perform measurements only in the "Near field" region:

A.1	Record zero offset $(B_0)$ of the Teslameter without any magnet nearby. Subtract subsequent field measurement with this value.	0.1 pt.
A.2	Measure magnetic field $B$ vs. $x$ in the near field region ( $7 \le x \le 16$ mm)! Where $x$ is the position measured from the center of the magnet. Record and plot your result on the answer sheet. Follow the "HINT & DIRECTIONS" below.	1.15 pt.
A.3	Use your experimental data to determine the value of the exponent $\boldsymbol{p}$ .	0.75 pt.
A.4	Determine the magnet's magnetization $M$ .	0.5 pt.

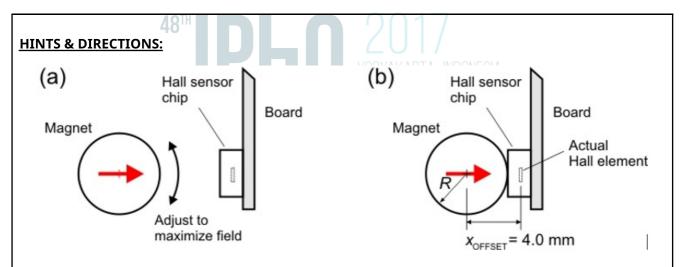
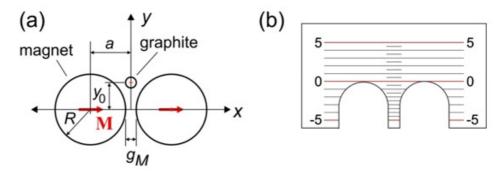


Figure 6. Magnetic field measurement (a) Adjustment (b) Offset issue

- 1. Turn off the Tesla meter if not in use to save battery!
- 2. For Teslameter, wait approximately ~2 sec for each data point before taking reading.
- 3. Note that x is measured from the center of magnet. Magnet radius is R = 3.2 mm.
- 4. Use recommended measurement setup in Fig. 5c.
- 5. See Fig. 6a, adjust the rotation of the magnet so its magnetization is pointing to the Hall sensor thus maximizing the field. You can use the yellow round sticker to mark the magnetization direction on the magnet.
- 6. When the Hall sensor touches the magnet the actual distance between the center of the magnet and the actual Hall sensor element is the offset value given as:  $x_{OFFSET} = 4 \text{ mm}$
- 7. Start your measurement with Hall sensor at x = 5 mm! Don't use the data when the sensor touches the magnet (x = 4 mm) as the sensor is saturated or the probe is flexing during touch.

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### [2] The Magnetic Levitation effect and Magnetic Susceptibility ( $\chi$ ) (1 pt.)



**Figure 7.** (a) The magnetic levitation effect in the PDL trap. (b) Insert ruler for measuring the levitation height  $y_0$ .

The PDL trap also demonstrates magnetic levitation effect. The graphite levitates at the center of the trap at height  $y_0$  as shown in Fig. 7(a). The graphite is repelled by the magnet with a force  $F_M(y_0)$  that depends on the magnetic susceptibility  $\chi$  and the rod position  $y_0$ . Magnetic susceptibility describes how much a material gets magnetized in response to an applied field. It appears in relation:  $\mu = (1+\chi)\mu_0$  where  $\mu$  is the magnetic permeability of the material. This magnetic repulsion force on a graphite rod in the PDL trap is given as:

$$F_M(y_0) = -\frac{\mu_0 M^2 \chi V_r}{2} \frac{R^4}{a^5} f\left(\frac{y_0}{a}\right)$$
 (3)

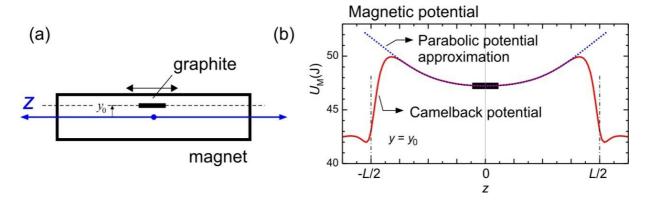
Note that when  $F_M(y_0)$  is positive the force is directed upwards and there is <u>a negative sign</u> in the formula. Here  $V_r$  is the volume of the graphite rod, M is the volume magnetization of the magnet (obtained from Question 1), a is the position of the magnet center given as:  $a = R + g_M/2$  (see Fig. 7a) where  $g_M$  is the gap between magnets:  $g_M$  = 1.5 mm. f(u) is the dimensionless function for the magnetic repulsion force in this trap given as:

$$f(u) = \frac{4u(3-u^2)(1-u^2)}{(1+u^2)^5} \tag{4}$$

A.5	Place gently a graphite rod HB/0.5 and length = 8 mm. Measure the levitation height $y_0$ of the rod (see Fig. 7a)! Hint: Use the insert ruler provided as shown in Fig. 7b. Press the ruler on the magnets to read the position of the graphite rod.	0.1 pt.
A.6	Use the result from part A.5 to determine the magnetic susceptibility $\chi$ of the graphite rod.	0.8 pt.
A.7	What kind of magnetic material is graphite? Choose one: (i) Ferromagnetic; (ii) Paramagnetic; or (iii) Diamagnetic?	0.1 pt.

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### [3] The camelback potential oscillation and magnetic susceptibility ( $\chi$ ) (1 pts)



**Figure 8.** (a) Graphite oscillation at height  $y_0$ . (b) The camelback potential of the PDL trap and its parabolic approximation.

We will determine  $\chi$  independently using the oscillation in the magnetic "camelback potential" of the PDL trap as shown in Fig. 8. For small amplitude (z < 4 mm) the magnetic potential can be approximated as a parabolic (shown as dotted curve in Fig. 8b):

$$U_M = \frac{1}{2}k_z z^2 \tag{5}$$

where  $k_z$  is the spring constant of the potential and z is center of mass displacement of the rod. This spring constant  $k_z$  depends on the magnet magnetization M (from Question 1) and  $\chi$ :

$$k_z = -C_1 \mu_0 \chi M^2 V_r \tag{6}$$

where  $\mu_0$  is the magnetic permeability,  $V_r$  is the volume of the graphite rod,  $C_1$  = 198.6 /m<sup>2</sup> is a constant for this magnetic trap setup.

Drop the graphite rod at the center of the magnetic trap. Adjust the platform level with the screw knobs so that the rod stays at the center of the trap. Displace the rod with a toothpick to induce oscillation along the camelback potential.

A.8	Perform an oscillation for the "HB/0.5" graphite and $l$ = 8 mm. Limit to small oscillation amplitude i.e. $A$ < 4mm. Determine the oscillation period. (The oscillation will decay over time due to damping, ignore this damping effect).	
A.9	Calculate the magnetic susceptibility ( $\chi$ ) of the graphite using this oscillation.	0.8 pt.

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#### [4] Oscillator quality factor (Q) and estimate of air viscosity (3 pt.)

We observe that the graphite rod oscillation is damped due to the air friction and we want to understand how the friction depends on the size of the graphite rod (diameter and length) and estimate the air viscosity  $\mu_A$ . The motion of the rod can be modeled as underdamped oscillation:  $z(t) = Ae^{-t/\tau}sin(\omega t)$  as shown in Fig. 3(a) where A is the initial amplitude and  $\omega = 2\pi f$  is the angular frequency and t is time. The amplitude decays with time by a factor of  $\exp(-t/\tau)$  where  $\tau$  is the damping time constant. This determines the oscillator "quality factor" defined as:  $Q = \omega \tau/2$ . If Q > 0.5 the oscillation is underdamped, Q = 0.5 is critically damped and Q < 0.5 is overdamped. This quality factor is important for designing PDL trap as seismometer or tiltmeter sensors.

We can calculate the damping time constant  $\tau$  by approximating the cylinder rods as long ellipsoid and calculate the Stokes drag force. The damping time constant is given as:

$$\tau = \frac{2}{3} \frac{\rho r^2}{\mu_A} ln \left( 0.607 \times \frac{l}{r} \right)$$
 (7)

where  $\rho$  , r and l are the mass density, radius and length of the graphite rod and  $\mu_A$  is the viscosity of the air. We want to estimate the air viscosity using this model graphical model of the model of th

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A.10	We need to determine the damping time constant of the oscillation $ au$ . Sketch how you measure $ au$ in <i>a simple way.</i>	0.5 pt.
A.11	Perform oscillation damping expe <i>r</i> iments with a group of rods with various diameters and fixed length of 8 mm. Determine the damping time constant $\tau$ for each rods.	1.5 pt.
A.12	Determine the air viscosity $\mu_A$ .	1.0 pt.

#### **SECTION B. SENSOR APPLICATIONS**

#### [5] PDL Trap Seismometer (0.5 pt.)

Imagine you are designing seismometer using this PDL magnetic trap. For seismometer application we want very high sensitivity or *very low acceleration "noise floor"* i.e. the lowest acceleration that it can detect. This acceleration noise floor is given as (in unit of  $m/(s^2Hz^{0.5})$ ):

$$a_n = \sqrt{\frac{4k_B T\omega}{Qm_R}} \tag{8}$$

where  $k_B$  is the Boltzmann constant, T is the temperature (see Constants and Data), and  $m_R$  is the mass of the rod, all are in SI units. In Question 4 in you have measured  $\tau$  of several graphite diameters. Pick one that you think will serve as the best seismometer.

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B.1	Which diameter of rod do you choose?	0.2 pt.
B.2	Calculate the seismometer acceleration noise floor $(a_n)$ for the rod of your choice.	0.3 pt.

## [6] PDL Trap Tiltmeter (2 pt.)

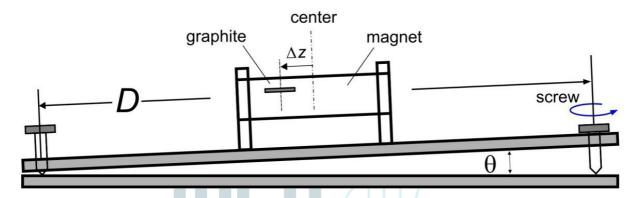


Figure 9. PDL trap system as tiltmeter

We will investigate the PDL trap as a very sensitive tiltmeter to monitor volcano. The change in the ground inclination is simulated by turning the screw and we want to determine the screw thread size S where S is the change of height per unit turn. We show that by measuring displacement of the graphite rod in the trap we can measure the inclination (tilt) precisely.

Use pencil rod HB/0.5 and length  $l=8\,$  mm in this experiment. Start from the center position. Assume the camelback potential can be approximated as harmonic potential like in problem 3:

B.3	Derive the relation theoretically between displacement $\Delta z$ with the screw thread size $S$ and the number of turns ( $N$ ).	0.5 pt.
B.4	By turning the screw slowly, determine the rod displacement $\Delta z$ vs. the number of screw turns ( $N$ ). Determine the thread size $S$ .	1.25 pt.
B.5	When the ground tilt changes we want the graphite rod to go to equilibrium as fast as possible (instead of sustaining very long oscillation) to allow easy reading. What is the ideal ${\it Q}$ factor for a tiltmeter?	0.25 pt.