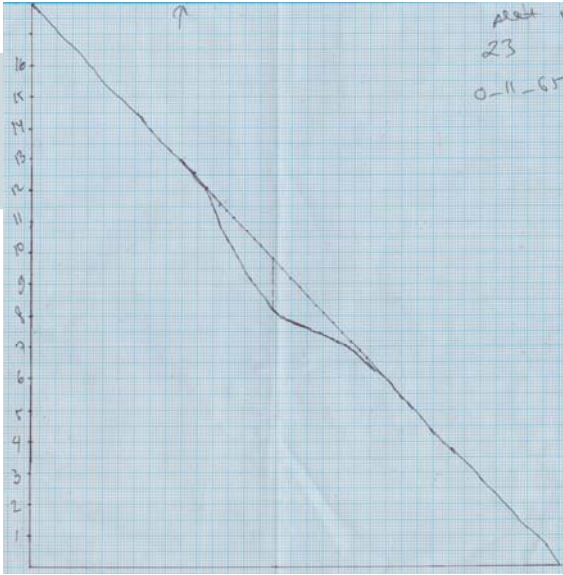


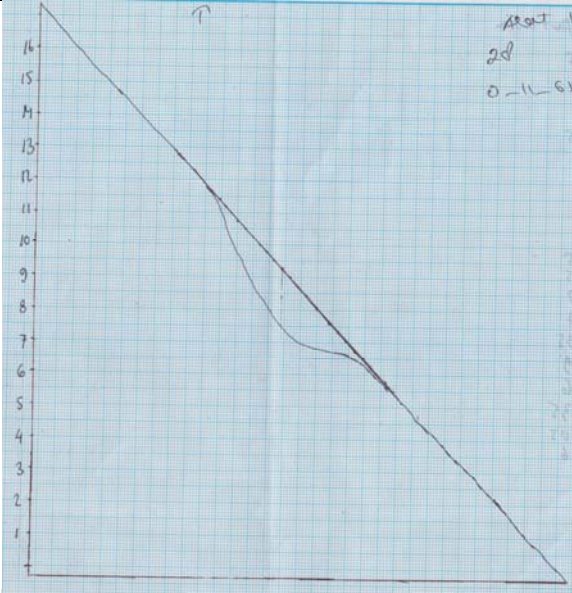
**Determination of Refractive Index Gradient and Diffusion
Coefficient of Salt Solution from Laser Deflection Measurement**

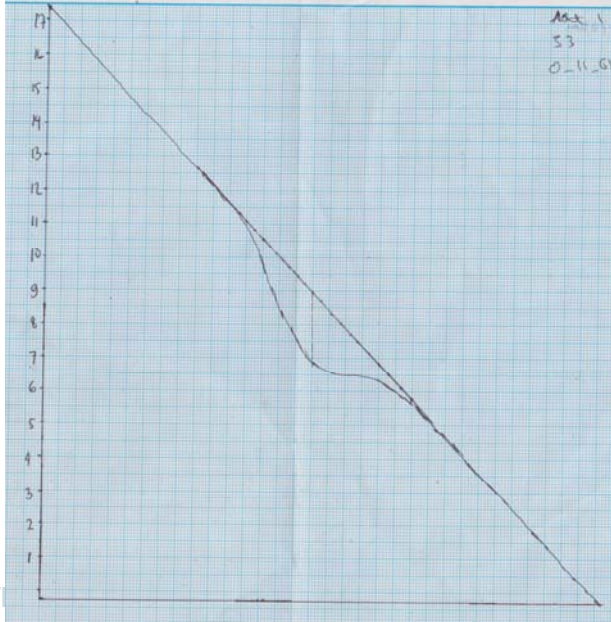
(10 points)

A. Measurement of Refractive Index Gradient of Salt Water Solution

(4.5 points)

Question	Answer	Marks
<p>A1. (1.2 pts)</p>	 <p>No dip</p> <p>No reference line</p> <p>Deflectogram (DL) not at the centre (+- 5mm) but the depth of dip still in 1.5 - 1.6 cm range</p> <p>DL at the centre, the depth of dip <1.5 cm or >1.6 cm</p> <p>DL not at the centre, the depth of dip <1.5 cm or >1.6 cm</p>	<p>Deflectogram of $C_0 = 23 \text{ g/150 mL}$</p> <p>Centred</p> <p>Depth of dip: 1.5 - 1.6 cm (0.4 pts)</p> <p>-0.4</p> <p>-0.05</p> <p>-0.05</p> <p>-0.05</p> <p>-0.1</p>
		Deflectogram

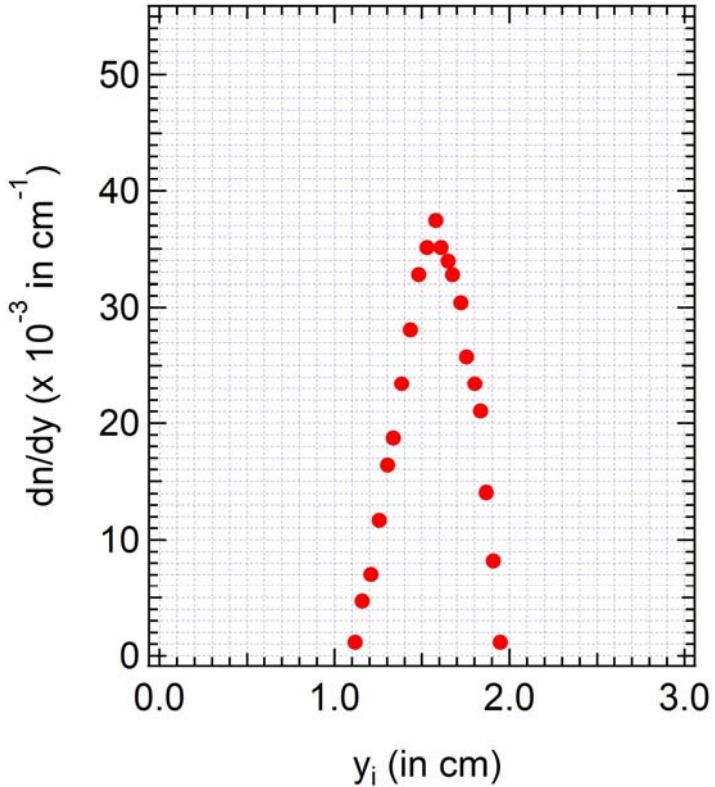
<p>A1.</p>	 <p>No dip</p> <p>No reference line</p> <p>Deflectogram (DL) not at the centre (+- 5mm) but the depth of dip still in 1.7 cm - 1.9 cm range</p> <p>DL at the centre, the depth of dip <1.7 cm or >1.9 cm</p> <p>DL not at the centre, the depth of dip <1.7 cm or >1.9 cm</p>	<p>of</p> <p>$C_0 = 28 \text{ gr}/150 \text{ mL}$</p> <p>Centred</p> <p>Deep of dip: 1.7 - 1.9 cm (0.4 pts)</p> <p>-0.4</p> <p>-0.05</p> <p>-0.05</p> <p>-0.05</p> <p>-0.1</p>
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<p>A1.</p>	 <p>No dip</p> <p>No reference line</p> <p>Deflectogram (DL) not at the centre (+-5mm) but the depth of dip still in 1.9 - 2.3 cm range</p> <p>DL at the centre, the depth of dip <1.9 cm or >2.3 cm</p> <p>DL not at the centre, the depth of dip <1.9 cm or >2.3 cm</p>	<p>Deflectogram of</p> <p>$C_0 = 33 \text{ g/150 mL}$</p> <p>Deep of dip: 1.9 - 2.3 cm</p> <p>(0.4 pts)</p> <p>-0.4 pts</p> <p>-0.05 pts</p> <p>- 0.05 pts</p> <p>- 0.05 pts</p> <p>-0.1</p>																																																																																																
<p>A2. (1.5 pts)</p>	<table border="1" data-bbox="400 1480 1177 2033"> <thead> <tr> <th>i</th> <th>$\delta_i \text{ (cm)}$</th> <th>$\xi_i \text{ (cm)}$</th> <th>$Z_0 \text{ (cm)}$</th> <th>$d \text{ (cm)}$</th> <th>$Z \text{ (cm)}$</th> </tr> </thead> <tbody> <tr><td>1</td><td>0.05</td><td>11.55</td><td>10.4 ± 0.1</td><td>0.8 ± 0.1</td><td>53.4 ± 0.1</td></tr> <tr><td>2</td><td>0.35</td><td>11.3</td><td></td><td></td><td></td></tr> <tr><td>3</td><td>0.6</td><td>11.05</td><td></td><td></td><td></td></tr> <tr><td>4</td><td>0.9</td><td>10.85</td><td></td><td></td><td></td></tr> <tr><td>5</td><td>1</td><td>10.65</td><td></td><td></td><td></td></tr> <tr><td>6</td><td>1.1</td><td>10.35</td><td></td><td></td><td></td></tr> <tr><td>7</td><td>1.3</td><td>10.15</td><td></td><td></td><td></td></tr> <tr><td>8</td><td>1.4</td><td>9.85</td><td></td><td></td><td></td></tr> <tr><td>9</td><td>1.45</td><td>9.7</td><td></td><td></td><td></td></tr> <tr><td>10</td><td>1.5</td><td>9.45</td><td></td><td></td><td></td></tr> <tr><td>11</td><td>1.6</td><td>9.25</td><td></td><td></td><td></td></tr> <tr><td>12</td><td>1.5</td><td>8.95</td><td></td><td></td><td></td></tr> <tr><td>13</td><td>1.4</td><td>8.65</td><td></td><td></td><td></td></tr> <tr><td>14</td><td>1.2</td><td>8.35</td><td></td><td></td><td></td></tr> <tr><td>15</td><td>1</td><td>8.05</td><td></td><td></td><td></td></tr> </tbody> </table>	i	$\delta_i \text{ (cm)}$	$\xi_i \text{ (cm)}$	$Z_0 \text{ (cm)}$	$d \text{ (cm)}$	$Z \text{ (cm)}$	1	0.05	11.55	10.4 ± 0.1	0.8 ± 0.1	53.4 ± 0.1	2	0.35	11.3				3	0.6	11.05				4	0.9	10.85				5	1	10.65				6	1.1	10.35				7	1.3	10.15				8	1.4	9.85				9	1.45	9.7				10	1.5	9.45				11	1.6	9.25				12	1.5	8.95				13	1.4	8.65				14	1.2	8.35				15	1	8.05				<p>Table 1 of</p> <p>$C_0 = 23 \text{ g/150 mL}$</p> <p>Optimum Z and Z_0</p> <p># data = 20</p> <p>(0.5 pts)</p>
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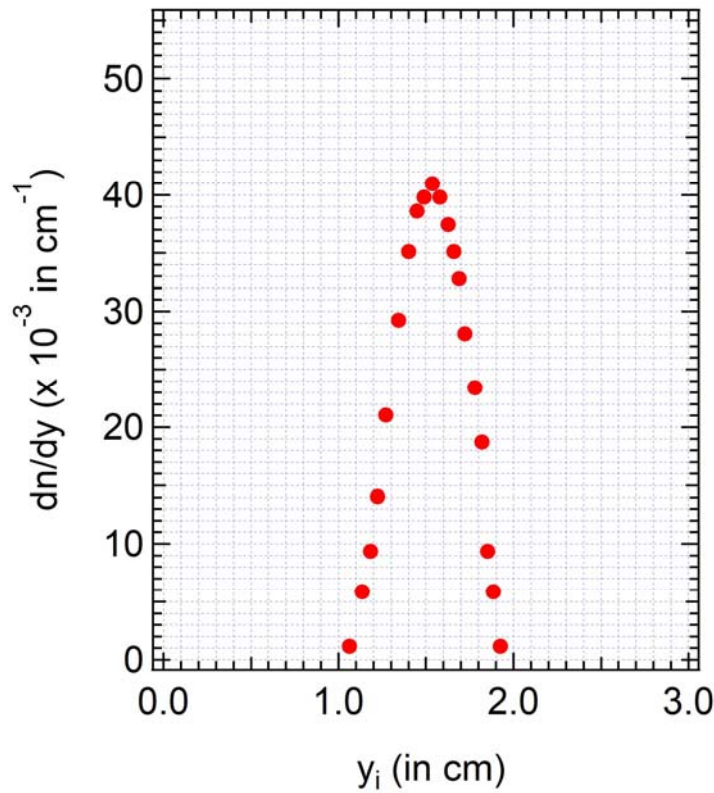
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<p>A3. (1.5 pts)</p>	<table border="1"> <thead> <tr> <th>i</th> <th>Y_i (cm)</th> <th>dn/dY</th> </tr> </thead> <tbody> <tr><td>1</td><td>1.85944</td><td>0.00117</td></tr> <tr><td>2</td><td>1.81919</td><td>0.00819</td></tr> <tr><td>3</td><td>1.77894</td><td>0.01404</td></tr> <tr><td>4</td><td>1.74674</td><td>0.02106</td></tr> <tr><td>5</td><td>1.71455</td><td>0.02340</td></tr> <tr><td>6</td><td>1.66625</td><td>0.02574</td></tr> <tr><td>7</td><td>1.63405</td><td>0.03043</td></tr> <tr><td>8</td><td>1.58575</td><td>0.03277</td></tr> <tr><td>9</td><td>1.56161</td><td>0.03394</td></tr> <tr><td>10</td><td>1.52136</td><td>0.03511</td></tr> <tr><td>11</td><td>1.48916</td><td>0.03745</td></tr> <tr><td>12</td><td>1.44086</td><td>0.03511</td></tr> <tr><td>13</td><td>1.39257</td><td>0.03277</td></tr> <tr><td>14</td><td>1.34427</td><td>0.02809</td></tr> <tr><td>15</td><td>1.29597</td><td>0.02340</td></tr> <tr><td>16</td><td>1.24767</td><td>0.01872</td></tr> <tr><td>17</td><td>1.21548</td><td>0.01638</td></tr> <tr><td>18</td><td>1.16718</td><td>0.01170</td></tr> <tr><td>19</td><td>1.11888</td><td>0.00702</td></tr> <tr><td>20</td><td>1.07058</td><td>0.00468</td></tr> <tr><td>21</td><td>1.03034</td><td>0.00117</td></tr> </tbody> </table> <p>Jury must check the data in table</p> <p># wrong data point < 3</p> <p>3<# wrong data point < 6</p> <p># wrong data point > 6</p>	i	Y _i (cm)	dn/dY	1	1.85944	0.00117	2	1.81919	0.00819	3	1.77894	0.01404	4	1.74674	0.02106	5	1.71455	0.02340	6	1.66625	0.02574	7	1.63405	0.03043	8	1.58575	0.03277	9	1.56161	0.03394	10	1.52136	0.03511	11	1.48916	0.03745	12	1.44086	0.03511	13	1.39257	0.03277	14	1.34427	0.02809	15	1.29597	0.02340	16	1.24767	0.01872	17	1.21548	0.01638	18	1.16718	0.01170	19	1.11888	0.00702	20	1.07058	0.00468	21	1.03034	0.00117	<p>Table 2 of</p> <p>C₀ = 23 g/150 mL.</p> <p># data = 20</p> <p>(0.25 pts)</p> <p>- 0</p> <p>- 0.05 pts</p> <p>- 0.25pts</p>
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<p>A3.</p>	 <p>No x-axis label -0.01 pts</p> <p>No x-axis unit -0.01 pts</p> <p>Without x-axis unit -0.01 pts</p> <p>No y-axis label -0.01 pts</p> <p>No y-axis unit -0.01 pts</p> <p>Without y-axis unit -0.01 pts</p> <p>Ordinate axis represented in 2 digid behind point -0.05 pts</p> <p>Ordinate axis represented in 3 digid behind point -0 pts</p> <p>Random shape -0.25 pts</p>	<p>Plot dn/dY vs Y</p> <p>$C_0 = 23 \text{ g}/150 \text{ mL}$.</p> <p>“Gaussian-Like” shape</p> <p>(0.25 pts)</p>															
<p>A3.</p>	<table border="1" data-bbox="399 1836 790 2016"> <thead> <tr> <th>i</th> <th>Y_i (cm)</th> <th>dn/dY</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>1.87554</td> <td>0.00117</td> </tr> <tr> <td>2</td> <td>1.83529</td> <td>0.00585</td> </tr> <tr> <td>3</td> <td>1.80309</td> <td>0.00936</td> </tr> <tr> <td>4</td> <td>1.77089</td> <td>0.01872</td> </tr> </tbody> </table>	i	Y_i (cm)	dn/dY	1	1.87554	0.00117	2	1.83529	0.00585	3	1.80309	0.00936	4	1.77089	0.01872	<p>Table 2 of</p> <p>$C_0 = 28 \text{ g}/150 \text{ mL}$.</p> <p># data = 20</p>
i	Y_i (cm)	dn/dY															
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without x-axis label

without x-axis unit

wrong x-axis unit

without y-axis label

without y-axis unit

wrong y-axis unit

Ordinate axis represented in 2 digid behind point

Ordinate axis represented in 3 digid behind point

Random shape of the curve

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.05 pts

-0 pts

-0.25 pts

A3.

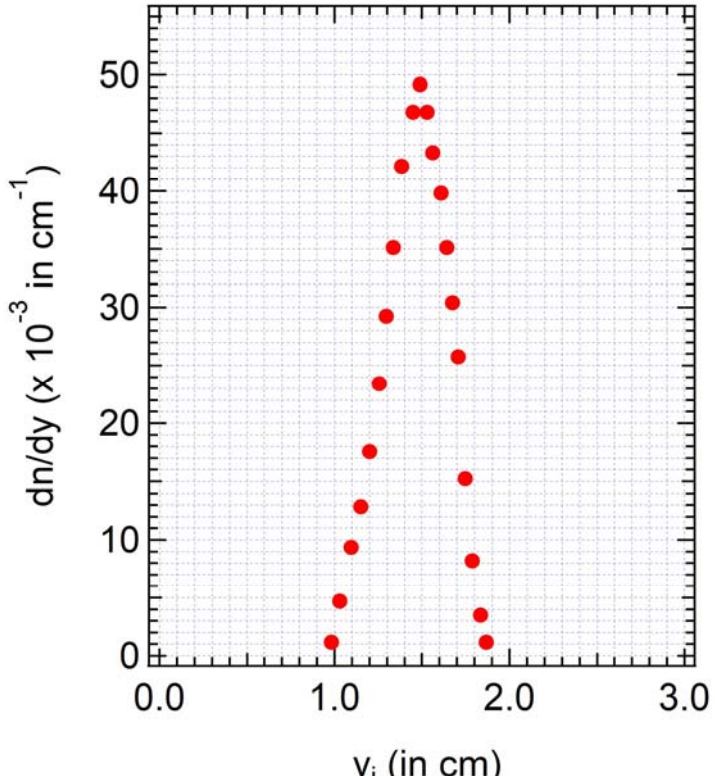
i	Y _i (cm)	dn/dY
1	1.86749	0.00117
2	1.83529	0.00351
3	1.78699	0.00819
4	1.74674	0.01521
5	1.70650	0.02574

Table 2 of

C₀ = 33 g/150 mL.

data = 20

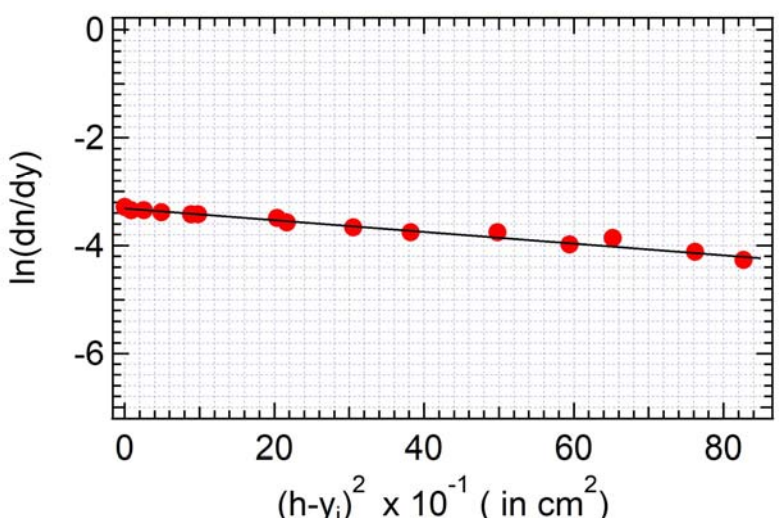
	<table border="1"> <tbody> <tr><td>6</td><td>1.67430</td><td>0.03043</td></tr> <tr><td>7</td><td>1.64210</td><td>0.03511</td></tr> <tr><td>8</td><td>1.60990</td><td>0.03979</td></tr> <tr><td>9</td><td>1.56161</td><td>0.04330</td></tr> <tr><td>10</td><td>1.52941</td><td>0.04681</td></tr> <tr><td>11</td><td>1.48916</td><td>0.04915</td></tr> <tr><td>12</td><td>1.44891</td><td>0.04681</td></tr> <tr><td>13</td><td>1.38452</td><td>0.04213</td></tr> <tr><td>14</td><td>1.33622</td><td>0.03511</td></tr> <tr><td>15</td><td>1.29597</td><td>0.02926</td></tr> <tr><td>16</td><td>1.25572</td><td>0.02340</td></tr> <tr><td>17</td><td>1.19938</td><td>0.01755</td></tr> <tr><td>18</td><td>1.15108</td><td>0.01287</td></tr> <tr><td>19</td><td>1.09473</td><td>0.00936</td></tr> <tr><td>20</td><td>1.03034</td><td>0.00468</td></tr> <tr><td>21</td><td>0.98204</td><td>0.00117</td></tr> </tbody> </table> <p>48th IPHO 2017 YOGYAKARTA-INDONESIA 16 - 24 JULY 2017</p> <p>Jury must check the data in table</p> <p># wrong data point < 3 - 0</p> <p>3 < # wrong data point < 6 - 0.05 pts</p> <p># wrong data point > 6 - 0.25pts</p>	6	1.67430	0.03043	7	1.64210	0.03511	8	1.60990	0.03979	9	1.56161	0.04330	10	1.52941	0.04681	11	1.48916	0.04915	12	1.44891	0.04681	13	1.38452	0.04213	14	1.33622	0.03511	15	1.29597	0.02926	16	1.25572	0.02340	17	1.19938	0.01755	18	1.15108	0.01287	19	1.09473	0.00936	20	1.03034	0.00468	21	0.98204	0.00117	(0.25 pts)
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<p>A4. (0.3 pts)</p>	<p>h for 23 g/ 150 mL = (1.5 ± 0.1) cm</p>	<p>0.1 pts</p>

	h for 28 g/ 150 mL = (1.5 ± 0.1) cm	0.1 pts
	h for 33 g/ 150 mL = (1.5 ± 0.1) cm	0.1 pts
	If h is correctly determined from graph A3 for each concentration	- 0
	If h is not correctly determined from graph A3 for each concentration	-0.1

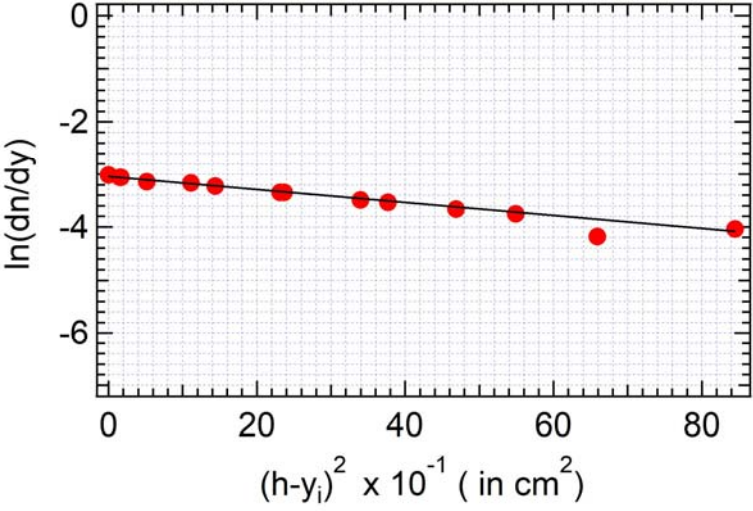
B : Determination of Diffusion Coefficient (4.2 points)

Question	Answer	Marks												
B1. (0.9 pts)	<p>Linear form of eq.(3)</p> $\ln\left(\frac{dn}{dy}\right) \approx m(h - Y)^2 + C \quad (b1)$ $m = -\frac{1}{4D_e t}$ <p>Constant : $C = \ln\left(\left(\frac{dn}{dc}\right)\left(\frac{c_0}{2\sqrt{\pi D_e t}}\right)\right)$</p> <p>Other than (b1)</p>	0.9 pt -0.9 pts												
B2. (1.8 pts)	<table border="1"> <thead> <tr> <th>i</th> <th>(h-y_i)²</th> <th>ln(dn/dy)</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0.06592</td> <td>-3.86003</td> </tr> <tr> <td>2</td> <td>0.050423</td> <td>-3.75467</td> </tr> <tr> <td>3</td> <td>0.031065</td> <td>-3.65936</td> </tr> </tbody> </table>	i	(h-y _i) ²	ln(dn/dy)	1	0.06592	-3.86003	2	0.050423	-3.75467	3	0.031065	-3.65936	Table 3 of C ₀ = 23 g /150 mL.
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13	0.05872	-3.97781																														
B2	 <p>Using linear regression of eq. (B1.1), we obtain</p> <p>m (slope) = -10 cm^{-2} till -8.8 cm^{-2}</p>	<p>Plot of Table 3</p> <p>$C_0 = 23 \text{ g/150 mL}$</p> <p># data = 10</p> <p>(0.3pts)</p>																														

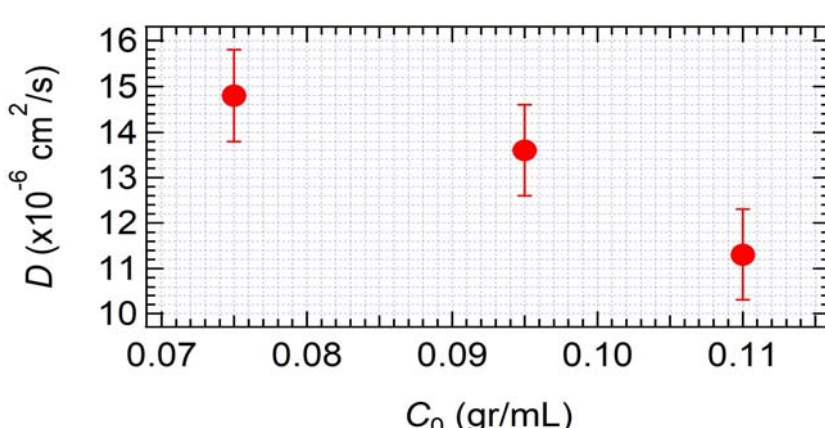
	<p>without x-axis label</p> <p>without x-axis unit</p> <p>wrong x-axis unit</p> <p>without y-axis label</p> <p>without y-axis unit</p> <p>wrong y-axis unit</p> <p># of data point in linear range > 10</p> <p>3 <= # of data point in linear range < 10</p> <p># of data point in linear range < 3 or random shape of curve</p> <p>m is out of range</p>	<p>-0.01 pts</p> <p>-0.01 pts</p> <p>-0.01 pts</p> <p>-0.01 pts</p> <p>-0.01 pts</p> <p>-0.01 pts</p> <p>- 0</p> <p>- 0.05 pts</p> <p>- 0.25 pts</p> <p>-0.3 pts</p>																																										
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	<p># of data point in linear range > 10 -0.05 pts</p> <p>3 <= # of data point in linear range < 10 -0.3 pts</p> <p># of data point in linear range < 3 or random shape of curve -0.3 pts</p> <p>m is out of range</p>																																											
B2.	<table border="1"> <thead> <tr> <th>i</th> <th>(h-y_i)²</th> <th>ln(dn/dy)</th> </tr> </thead> <tbody> <tr><td>1</td><td>0.046873</td><td>-3.65936</td></tr> <tr><td>2</td><td>0.033968</td><td>-3.4923</td></tr> <tr><td>3</td><td>0.023136</td><td>-3.3492</td></tr> <tr><td>4</td><td>0.014378</td><td>-3.22404</td></tr> <tr><td>5</td><td>0.005128</td><td>-3.13948</td></tr> <tr><td>6</td><td>0.001553</td><td>-3.06152</td></tr> <tr><td>7</td><td>6.99E-07</td><td>-3.01273</td></tr> <tr><td>8</td><td>0.001688</td><td>-3.06152</td></tr> <tr><td>9</td><td>0.011126</td><td>-3.16688</td></tr> <tr><td>10</td><td>0.023647</td><td>-3.3492</td></tr> <tr><td>11</td><td>0.037646</td><td>-3.53152</td></tr> <tr><td>12</td><td>0.054884</td><td>-3.75467</td></tr> <tr><td>13</td><td>0.08446</td><td>-4.04235</td></tr> </tbody> </table> <p>Jury must check the data in table</p> <p># of data point > 10 -0 pts</p> <p>3 <= # of data point < 10 -0.05 pts</p> <p># of data point < 3 -0.3 pts</p> <p># wrong data point < 3 - 0</p> <p>3 < # wrong data point < 6 - 0.05 pts</p> <p># wrong data point > 6 - 0.25</p>	i	(h-y _i) ²	ln(dn/dy)	1	0.046873	-3.65936	2	0.033968	-3.4923	3	0.023136	-3.3492	4	0.014378	-3.22404	5	0.005128	-3.13948	6	0.001553	-3.06152	7	6.99E-07	-3.01273	8	0.001688	-3.06152	9	0.011126	-3.16688	10	0.023647	-3.3492	11	0.037646	-3.53152	12	0.054884	-3.75467	13	0.08446	-4.04235	<p>Table 3 of C₀ = 33 g /150 mL</p> <p># data = 10</p> <p>(0.3 pts)</p>
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B2.		<p>Plot of Table 3</p> <p>C₀ = 33 g/150 mL</p>																																										

	 <p>Using linear regression of eq. (B1.1), we obtain m (slope) = -11.3 cm^{-2} till -12.8 cm^{-2} without x-axis label without x-axis unit wrong x-axis unit without y-axis label without y-axis unit wrong y-axis unit</p> <p>m is out of range # of data point in linear range > 10 $3 \leq$ # of data point in linear range < 10 # of data point in linear range < 3 or random shape of curve</p>	<p># data = 10 (0.3pts) -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.3 pts -0 pts -0.05 pts -0.3</p>
<p>B3 (1.5 pts)</p>	<p>D of 23 g/ 150 mL = $(1.38 \text{ till } 1.58) \times 10^{-5} \text{ cm}^2/\text{s}$ D of 28 g/ 150 mL = $(1.26 \text{ till } 1.46) \times 10^{-5} \text{ cm}^2/\text{s}$</p>	<p>0.5 pts 0.5 pts</p>

	D of 33 g/ 150 mL = (1.03 till 1.23) $\times 10^{-5}$ cm ² /s D is out of range for each concentration	0.5 pts- -0.5 pts
--	--	----------------------

C. Nonlinear diffusion (1.3 points)

Question	Answer	Marks
C1. (1.3 pts)	 <p>Without error bars Value of C not stated in C₀/2</p>	Plot D vs. C_0 0.8 pts -0 -0.4 pts
C1.	$\frac{d}{dc}D = -4.2 \times 10^{-5} \text{cm}^2 \text{mL g}^{-1} \text{s}^{-1}$ till $-15.8 \times 10^{-5} \text{cm}^2 \text{mL g}^{-1} \text{s}^{-1}$	0.5 pts -0.01 pts -0.5 pts



E1. Marking Scheme & Solution

Student Code

Experimental
Question

1

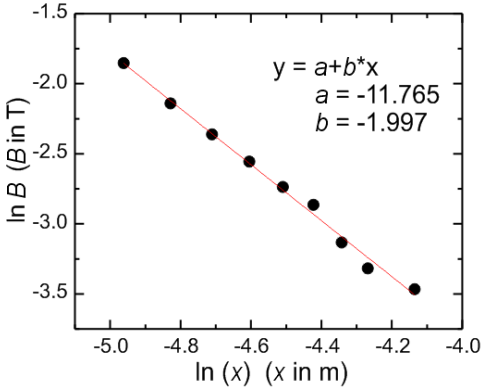
page 19 of 19



Parallel Dipole Line Magnetic Trap for Earthquake & Volcanic Sensing (10 points)

A. BASIC CHARACTERISTICS OF PDL TRAP

1. Determination of the magnet's magnetization (M) (2.5 pts)

Question	Answer	Marks																																																												
A.1 0.1 pts	<p>Record zero offset (B_0) of the Teslameter without any magnet nearby. Subtract subsequent field measurement with this value</p> <p>Example from a Teslameter unit: $B_0 = 0.86$ mT</p>	<p>0.08 pts range (-10 mT to 10 mT)</p> <p>Correct unit: 0.02 pts</p>																																																												
A.2 1.15 pts	<p>Measure magnetic field B vs. x in the near field region ($7 \leq x \leq 16$ mm). Where x is the position measured from the center of the magnet. Record and plot your result on the answer sheet.</p> <p>$x_0 = 4$ mm, $B_0 = 0.86$ mT. Δx is measured from surface. $B = B_{raw} - B_0$</p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>Δx (mm)</th> <th>X (mm)</th> <th>B_{raw} (T)</th> <th>B (T)</th> <th>$\ln(x)$ x in m</th> <th>$\ln(B)$ B in T</th> </tr> </thead> <tbody> <tr><td>3</td><td>7</td><td>0.1576</td><td>0.1567</td><td>-4.962</td><td>-1.853</td></tr> <tr><td>4</td><td>8</td><td>0.1186</td><td>0.1177</td><td>-4.828</td><td>-2.139</td></tr> <tr><td>5</td><td>9</td><td>0.0951</td><td>0.0942</td><td>-4.710</td><td>-2.362</td></tr> <tr><td>6</td><td>10</td><td>0.0785</td><td>0.0776</td><td>-4.605</td><td>-2.556</td></tr> <tr><td>7</td><td>11</td><td>0.0657</td><td>0.0648</td><td>-4.510</td><td>-2.736</td></tr> <tr><td>8</td><td>12</td><td>0.0579</td><td>0.0570</td><td>-4.423</td><td>-2.864</td></tr> <tr><td>9</td><td>13</td><td>0.0445</td><td>0.0436</td><td>-4.343</td><td>-3.132</td></tr> <tr><td>10</td><td>14</td><td>0.0371</td><td>0.0362</td><td>-4.269</td><td>-3.318</td></tr> <tr><td>12</td><td>16</td><td>0.0321</td><td>0.0312</td><td>-4.135</td><td>-3.466</td></tr> </tbody> </table> <p>Plot:</p> 	Δx (mm)	X (mm)	B_{raw} (T)	B (T)	$\ln(x)$ x in m	$\ln(B)$ B in T	3	7	0.1576	0.1567	-4.962	-1.853	4	8	0.1186	0.1177	-4.828	-2.139	5	9	0.0951	0.0942	-4.710	-2.362	6	10	0.0785	0.0776	-4.605	-2.556	7	11	0.0657	0.0648	-4.510	-2.736	8	12	0.0579	0.0570	-4.423	-2.864	9	13	0.0445	0.0436	-4.343	-3.132	10	14	0.0371	0.0362	-4.269	-3.318	12	16	0.0321	0.0312	-4.135	-3.466	<p>Correct label and unit for data: 0.1 pts</p> <p>Number of correct data for $x \leq 16$ mm: 0.05 pts for each correct data, max 0.45 pts</p> <p>Plot: -Correct axis label and unit: 0.05 pts - Using around 75% of plot area: 0.05 pts -For each correct data point: 0.05 pts, max. 0.4 pts -Adding trendline: 0.1 pts</p>
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<p>A.3 0.75 pts</p>	<p>Use your experimental data to determine the value of the exponent p.</p> <p>Linear regression (LR) $y = a + b x : B = \frac{\mu_0 m}{2 \pi L x^p}$</p> <p>$\ln(B) = a - p \ln x$ where $a = \ln\left(\frac{\mu_0 m}{2 \pi L}\right)$.</p> <p>LR yields : $a = -11.765$ and $b = -1.997$</p> <p>The power exponent: $p = -b = 2.0$</p> <p>Note that this is in very good agreement with the exact result: at short distance ($x < L$) a diametric (or a dipole line) magnet has $B \sim 1/r^2$ dependence. See Ref. [1] , Fig. 2c.</p>	<p>Obtaining p from graph: 0.05 pts Obtaining p from linear regression: 0.1 pts</p> <p>Result: $p = 1.8 - 2.2 : 0.65$ pts $p = 1.6 - 2.4 : 0.35$ pts</p> <p>Result with wrong sign: $p = (-1.8) - (-2.2) : 0.4$pts $p = (-1.6) - (-2.4) : 0.1$pts</p> <p>More than two sig. figs.: minus 0.05 pts</p>
<p>A.4 0.5 pts</p>	<p>Determine the magnet's magnetization M.</p> <p>$m = \frac{2 \pi L}{\mu_0} \exp(a) = 0.987 \text{ Am}^2$</p> <p>$M = \frac{m}{\pi R^2 L} = 1.2 \times 10^6 \text{ A/m}$</p> <p>This is close to the more accurate results from more extensive measurements to far field (see Ref. [1], Fig. 2c) and we use this value for subsequent questions: $M = 1.1 \times 10^6 \text{ A/m}$</p>	<p>Correct unit: 0.05 pts</p> <p>Obtaining intercept (a) from graph: 0.025 pts Obtaining intercept from LR: 0.05 pts</p> <p>Correct formula for m and/or M : 0.1 pts</p> <p>Result for M ($\times 10^6 \text{ A/m}$): $0.9 - 1.4 : 0.3$ pts $0.1 - 2.5 : 0.15$ pts</p> <p>More than 2 sig. figs.: minus 0.05 pts</p>

2. The Magnetic Levitation Effect and Magnetic Susceptibility (χ) (1 pts)

Question	Answer	Marks
<p>A.5 0.1 pts</p>	<p>Place gently a graphite rod HB/0.5 and length = 8 mm. Measure the levitation height y_0 of the rod (see Fig. 7a). Hint: Use the insert ruler provided as shown in Fig. 7b. Press the ruler on the magnets to read the position of the graphite rod</p> <p>We levitate graphite HB/0.5, $l = 8$ mm. Using the insert-ruler, we measure approximately $\Delta y = 1$ mm from the top of the magnet surface. Thus: $y_0 = R - \Delta y = (3.2 - 1) \text{ mm} = 2.2 \text{ mm}$</p>	<p>correct unit: 0.02</p> <p>$y_0 = (1.7 - 2.2) \text{ mm} : 0.08$ pts</p> <p>partial credit: Only $\Delta y = (1 - 1.5) \text{ mm} : 0.03$ pts</p>

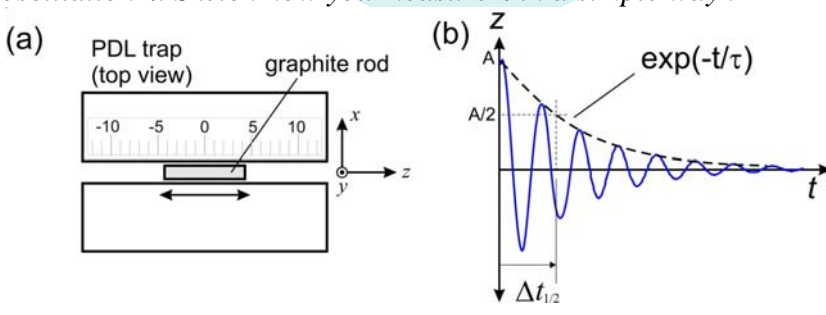
<p>A.6 0.8 pts</p>	<p>Use the result from part A.5 to determine the magnetic susceptibility χ of the graphite rod.</p> <p>Solving for χ: $mg = F_y = -\frac{\mu_0 M^2 \chi V_R R^4}{2 a^5} f_Y(y_0/a)$</p> $\chi = -\frac{2\rho g a^5}{\mu_0 M^2 R^4 f_Y(y_0/a)}$ <p>We calculate: $a = R + g_M / 2 = (3.2 + 1.5/2) \text{ mm} = 3.95 \text{ mm}$.</p> <p>Using $y_0 = 2.2 \text{ mm}$: $f_Y(u) = \frac{4u(3-u^2)(1-u^2)}{(1+u^2)^5}$,</p> $f_Y(y_0/a) = f_Y(2.2/3.95) = 1.07$ <p>Using the correct $M = 1.1 \times 10^6 \text{ A/m}$; and $R = 3.2 \text{ mm}$, $\rho = 1680 \text{ kg/m}^3$ we have: $\chi = -1.85 \times 10^{-4}$.</p> <p>Note that this is very good agreement with the literature value for graphite pencil lead: $\chi = -2 \times 10^{-4}$ (see Ref.[1], pg. 2 & Ref.[2]). The sign is negative indicating a diamagnetic material.</p>	<p>Correct expression for χ: 0.4 pts</p> <p>Result for χ ($\times 10^{-4}$) -(1.4 to 2.6) : 0.4 pts -(0.5 to 4) : 0.2 pts</p> <p>Wrong sign: minus 0.1 pts</p>
<p>A.7 0.1 pts</p>	<p>What kind of magnetic material is graphite? Choose one: (i) Ferromagnetic; (ii) Paramagnetic; or (iii) Diamagnetic?</p> <p>(iii) Diamagnetic. Because: (1) Graphite is repelled by magnetic field (2) The sign of χ is negative.</p>	<p>Correct choice: 0.1 pts</p>

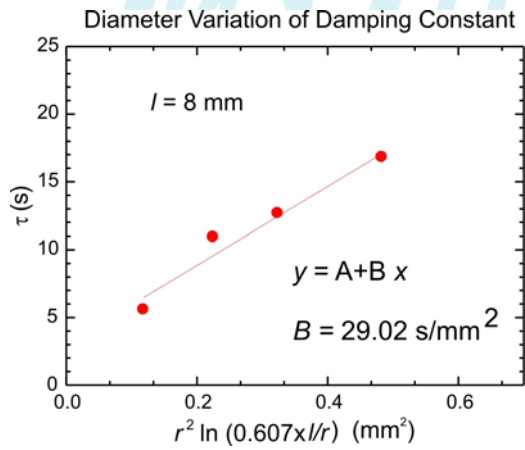
3. The camelback potential oscillation and magnetic susceptibility (χ) (1 points)

Question	Answer	Marks																		
<p>A.8 0.2 pts</p>	<p><u>Perform an oscillation for the "HB/0.5" graphite and $l = 8 \text{ mm}$. Limit to small oscillation amplitude i.e. $A < 4 \text{ mm}$.</u></p> <p><u>Determine the oscillation period. (The oscillation will decay over time due to damping, ignore this damping effect).</u></p> <p>Example, we measured 5 oscillations of HB/0.5 with length $l = 8 \text{ mm}$. We displaced it by $\sim 3 \text{ mm}$ and let it oscillates. We measured 5 oscillation periods:</p> <table border="1" data-bbox="300 1926 1077 2033"> <thead> <tr> <th>Trial</th> <th>5 T_z</th> <th></th> <th></th> <th></th> <th></th> </tr> </thead> <tbody> <tr> <td></td> <td>(s)</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>1</td> <td>6.12</td> <td></td> <td></td> <td></td> <td></td> </tr> </tbody> </table>	Trial	5 T_z						(s)					1	6.12					<p>Correct label and unit: 0.02 pts</p> <p>Number of correct data each 0.01 pts, max 0.03 pts</p> <p>Number of oscillation < 3 : 0 pts ≥ 3 : 0.05 pts</p> <p>$T_z = (1.2 - 1.5) \text{ s}$: 0.1 pts</p>
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2	6.13													
3	6.14													
A.9 0.8 pts	<p>Calculate the magnetic susceptibility (χ) of the graphite using this oscillation</p> <p>For harmonic oscillator : $k_z = m_R \omega^2$, solving for χ:</p> $\chi = -\frac{k_z}{C_1 \mu_0 M^2 V_r} = \frac{\omega^2 \rho}{C_1 \mu_0 M^2}$ <p>Using the correct $M = 1.1 \times 10^6$ A/m. Using $C_1 = 198.6/\text{m}^2$, and $T_z = 1.23$ s, we obtain $\chi = -1.5 \times 10^{-4}$.</p> <p>Note that this is in good agreement with the literature value of the graphite pencil lead: $\chi = -2 \times 10^{-4}$ (Ref.[1], pg. 2); and the sign is negative indicating a diamagnetic material.</p>	<p>Correct expression for χ: 0.4 pts</p> <p>Result for χ ($\times 10^{-4}$) -(1.4 to 2.6) : 0.4 pts -(0.5 to 4) : 0.2 pts</p> <p>Wrong sign: minus 0.1 pts</p>												

4. Oscillator quality factor (Q) and estimate of air viscosity μ_A (3.0 points)

Question	Answer	Marks
A.10 0.5 pts	<p>We need to determine the damping time constant of the oscillation τ. Sketch how you measure τ in a simple way.</p>  <p>The trick is to use "half-time" concept of exponential decay. We set the oscillation and measure the time taken for the amplitude to halve. The lifetime is:</p> $\tau = \frac{\Delta t_{1/2}}{\ln 2}$	<p>Correct idea: 0.3 pts</p> <p>Correct expression for τ: 0.2 pts</p>
A.11 1.5 pts	<p>Perform oscillation damping experiments with a group of rods with various diameters and fixed length of 8 mm. Determine the damping time constant τ for each rods</p>	<p>Correct label and unit 0.1</p> <p>Number of correct data</p>

	<p>We displaced the graphite by ~4 mm, started the stopwatch and then waited until it decays to half.</p> <table border="1" data-bbox="300 398 1131 987"> <thead> <tr> <th>Trial</th> <th>Diam.</th> <th>Actual Radius</th> <th>$\Delta t_{1/2}$</th> <th>Mean $\Delta t_{1/2}$</th> <th>τ</th> <th>$r^2 \times \ln(0.607/l/r)$</th> </tr> <tr> <td></td> <td>(mm)</td> <td>(mm)</td> <td>(s)</td> <td>(s)</td> <td>(s)</td> <td>(mm²)</td> </tr> </thead> <tbody> <tr> <td>1</td> <td>0.3</td> <td>0.19</td> <td>3.89</td> <td>3.913</td> <td>5.646</td> <td>0.117</td> </tr> <tr> <td></td> <td></td> <td></td> <td>3.97</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>3.88</td> <td></td> <td></td> <td></td> </tr> <tr> <td>2</td> <td>0.5</td> <td>0.28</td> <td>7.69</td> <td>7.617</td> <td>10.989</td> <td>0.224</td> </tr> <tr> <td></td> <td></td> <td></td> <td>7.57</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>7.59</td> <td></td> <td></td> <td></td> </tr> <tr> <td>3</td> <td>0.7</td> <td>0.35</td> <td>8.77</td> <td>8.82</td> <td>12.73</td> <td>0.322</td> </tr> <tr> <td></td> <td></td> <td></td> <td>8.81</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>8.88</td> <td></td> <td></td> <td></td> </tr> <tr> <td>4</td> <td>0.9</td> <td>0.45</td> <td>12.4</td> <td>11.70</td> <td>16.88</td> <td>0.482</td> </tr> <tr> <td></td> <td></td> <td></td> <td>11.33</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td>11.38</td> <td></td> <td></td> <td></td> </tr> </tbody> </table>	Trial	Diam.	Actual Radius	$\Delta t_{1/2}$	Mean $\Delta t_{1/2}$	τ	$r^2 \times \ln(0.607/l/r)$		(mm)	(mm)	(s)	(s)	(s)	(mm ²)	1	0.3	0.19	3.89	3.913	5.646	0.117				3.97							3.88				2	0.5	0.28	7.69	7.617	10.989	0.224				7.57							7.59				3	0.7	0.35	8.77	8.82	12.73	0.322				8.81							8.88				4	0.9	0.45	12.4	11.70	16.88	0.482				11.33							11.38				<p>for each diameter (4): < 3 : 0.1 pts >=3 : 0.25 pts (max 1.0 pts)</p> <p>Positive monotonic trend for τ vs. diameter from 0.3 to 0.9 mm with $\tau = 5$ to 20 sec : 0.4 pts</p>
Trial	Diam.	Actual Radius	$\Delta t_{1/2}$	Mean $\Delta t_{1/2}$	τ	$r^2 \times \ln(0.607/l/r)$																																																																																														
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<p>A.12 1 pts</p>	<p>Determine the air viscosity μ_A</p>  <p>We have: $\tau = b r^2 \ln\left(0.607 \times \frac{l}{r}\right)$, where: $b = \frac{2}{3} \frac{\rho}{\mu_A}$. We performed linear regression $y = a + b x$, with $y = \tau$ and $x = r^2 \ln\left(0.607 \times \frac{l}{r}\right)$. We obtain: $b = 29.02 \text{ s/mm}^2$.</p> $\mu_A = \frac{2}{3} \frac{\rho}{b} = 38.6 \cdot 10^{-6} \text{ Pa}\cdot\text{s} \quad (1 \text{ Pa}\cdot\text{s} = 1 \text{ kg/m}\cdot\text{s})$ <p>Note that this is about 2.1x the actual viscosity of air of $18.2 \mu\text{Pa}\cdot\text{s}$. The discrepancy is due to the ellipsoidal</p>	<p>Correct unit: 0.05</p> <p>Obtaining result with linear regression or plot: 0.25 pts</p> <p>Result μ_A ($\times 10^{-6}$ Pa.s): 20 - 60 : 0.7 pts 10 - 80 : 0.4 pts 1 - 100 : 0.1 pts</p>																																																																																																		

	approximation of the Stokes drag (vs. the actual cylindrical shape of the rod) and the proximity effect of the rod to the magnet (wall effect). Another factor is the crude nature of our manual τ determination. See Ref. [1], pg. 8.	
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B. SENSOR APPLICATION OF THE PDL TRAP

5. PDL Trap Seismometer (0.5 pts)

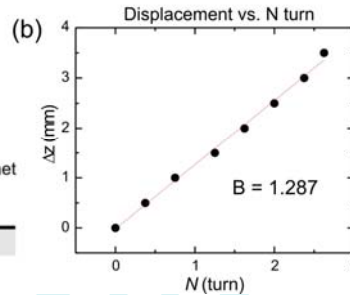
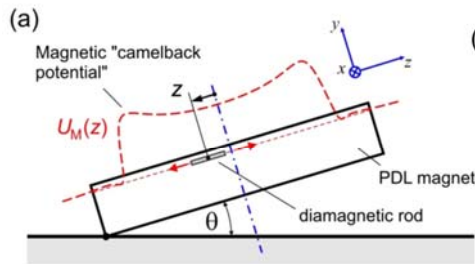
Question	Answer	Marks
B.1 0.2 pts	<p>Which diameter of rod do you choose?</p> <p>To obtain the lowest acceleration noise floor "a_n" we should choose the largest diameter graphite i.e. 0.9 mm, because their damping time is the longest and the mass is the largest.</p>	Correct answer: 0.2 pts
B.2 0.3 pts	<p>Calculate the seismometer acceleration noise floor (a_n) for the rod of your choice!</p> <p>For HB/0.9 and length $l = 8$ mm: We use $\tau = 16.9$ s; and $T = 298$ K, we have: $m_R = \rho \pi r^2 l = 8.55 \times 10^{-6}$ kg :</p> $a_n = \sqrt{\frac{4k_B T \omega_0}{Q m_R}} = \sqrt{\frac{8k_B T}{\tau m_R}} = 1.5 \times 10^{-8} \text{ m}/(\text{s}^2 \text{ Hz}^{0.5})$	<p>Correct unit: 0.1</p> <p>Correct answer: 0.2 pts</p>

6. PDL Trap Tiltmeter (2 pts)

Question	Answer	Marks
B.3 0.5 pts	<p>Derive the relation theoretically between displacement Δz with the screw thread size S and the number of turns (N).</p> $k_z \Delta z = m g \sin \theta = m g N S / D \quad \Delta z = \frac{m g S N}{k_z D}$ <p>From Question 3, we also have $k_z = m \omega^2$:</p> $\Delta z = \frac{g S}{\omega^2 D} N$	<p>Correct expression: 0.5 pts</p> <p>Partial credit $k_z \Delta z = m g \sin \theta : 0.2$</p>
B.4 1.25 pts	<p>By turning the screw slowly, determine the rod displacement Δz vs. the number of screw turns (N). Determine the thread size S</p>	Correct label and unit: 0.1 pts

We measured the distance between screws: $D = 22$ cm, and we used the period from Q3: $T_z = 1.23$ s

Δz (mm)	ϕ	N (turn)			
0	0	0			
0.5	135	0.375			
1	270	0.75			
1.5	450	1.25			
2	585	1.625			
2.5	720	2.0			
3	855	2.375			
3.5	945	2.625			



By performing linear regression: $y = a + b x$

We have $b = 1.287$ mm/turns : $S = \frac{b \omega^2 D}{g} = 0.75$ mm/turn.

This is reasonably close to the actual value of the thread size: $S = (0.8 \pm 0.1)$ mm/turn.

Distance between screws:
 $22.8 < D < 22.2$ cm :
0.1 pts

Number of correct data:
< 3 sets : 0 pts
3-5 sets: 0.15 pts
>5 sets : 0.25 pts

Obtaining result with
linear regression or plot:
0.2 pts

Result:
 $0.7 < S < 0.9$: 0.55 pts
 $0.5 < S < 1.1$: 0.15 pts

Correct unit for S :
0.05

B.5
0.25
pts

When the ground tilt changes we want the graphite rod to go to equilibrium as fast as possible (instead of sustaining very long oscillation) to allow easy reading. What is the ideal Q factor for a tiltmeter?

We need critical damping thus: $Q = 0.5$

Correct Q : 0.25 pts

REFERENCES:

- [1] Gunawan, O. & Virgus, Y. *The one-dimensional camelback potential in the parallel dipole line trap: Stability conditions and finite size effect.* J. Appl. Phys. 121, 133902, (2017). DOI:10.1063/1.4978876.
- [2] Gunawan, O., Virgus, Y. & Fai Tai, K. *A parallel dipole line system.* Appl. Phys. Lett. 106, 062407, (2015). DOI: 10.1063/1.4907931.